

1 High-Impact and Transformative Science (HITS) Metrics: Definition, Exemplification,  
2 and Comparison

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## 14 Abstract

15 Countries, research institutions, and scholars are interested in identifying and promoting high-impact  
16 and transformative scientific research. This paper presents novel metrics that use and extend  
17 bibliometric and linguistic approaches to identify high-impact and transformative works. The 11 general  
18 metrics can be grouped into seven types: Radical-Generative, Radical-Destructive, Risky,  
19 Multidisciplinary, Wide Impact, Growing Impact and High Impact. A total of 10,778,696 articles available  
20 in Thomson Reuters' Science Citation Index Expanded™ linked to MEDLINE are used to exemplify and  
21 validate the metrics. Publication years are grouped into six 5-year periods spanning 1983-2012 and  
22 6,159 comparable MeSH terms that characterize the fields to which each article belongs. The analysis is  
23 conducted at the level of a field-period pair, of which 15,051 have articles and are used in this study.  
24 Analysis show that transformativeness is positively related to impact ( $\rho=.401$ ), but no evidence that  
25 transformative work is adopted slowly or that the generation of important new concepts coincides with  
26 the obsolescence of existing concepts.

## 27 1. Introduction

28 Countries, research institutions, and scholars have prioritized high-impact and transformative scientific  
29 research. The National Science Board (NSB) argues that while research that has the potential to  
30 transform science “is inherently less predictable in its course and eventual outcomes, it is, nonetheless,  
31 absolutely essential for our national advancement and for the advancement of science as a whole (NSB,  
32 2007).”

33 Recognizing the importance of transformative research, the National Institutes of Health (NIH) and  
34 National Science Foundation (NSF) both instituted initiatives to support transformative research. Yet, no  
35 standard metrics exist to identify transformative research, which limits our ability to answer even basic  
36 questions about it. Such metrics are essential if we want to answer even such fundamental questions as:  
37 How frequent is transformative research? How important is transformative research for scientific  
38 progress? Does the prevalence of transformative research vary over time or across fields? To what  
39 extent do high impact and transformative work overlap? How do the demographics (in terms of gender,  
40 race, age, national origin) of fields, the structure of scientific networks, or the funding environment  
41 affect the production, diffusion, and reception of transformative research?

42 A National Science Board report from 2007 argues:

43 Science progresses in two fundamental and equally valuable ways: The vast majority of scientific  
44 understanding advances incrementally, with new projects building upon the results of previous  
45 studies or testing long-standing hypotheses and theories. This progress is evolutionary—it  
46 extends or shifts prevailing paradigms over time. The vast majority of research conducted in  
47 scientific laboratories around the world fuels this form of innovative scientific progress. Less  
48 frequently, scientific understanding advances dramatically, through the application of radically  
49 different approaches or interpretations that result in the creation of new paradigms or new  
50 scientific fields. This progress is revolutionary, for it transforms science by overthrowing  
51 entrenched paradigms and generating new ones. The research that comprises this latter form of  
52 scientific progress ... [is] termed transformative research... (National Science Board, 2007).

53 This paper develops metrics to identify those scientific fields and periods of time (“field-period pairs”) in  
54 which high-impact work and transformative work was done. We begin by grounding our work in  
55 established conceptualizations of transformative research from NIH, NSB, and NSF. These  
56 conceptualizations identify seven aspects of transformative work. Transformative work is seen to be:

57 radical in the sense of (1) generating important new ideas and (2) making existing ideas obsolete or less  
58 salient (3) risky, (4) multidisciplinary, (5) having a broad impact, (6) having an impact that builds over  
59 time, and (7) being high impact. We then develop eleven metrics that correspond to these aspects of  
60 transformative work using rich characterizations of citation patterns as well as natural language  
61 processing techniques. We next use factor analysis to identify the combination of our eleven metrics  
62 that best characterize the seven aspects of transformative work. Finally, we reduce the dimensionality  
63 of the metrics of transformativeness (other than impact) into a single measure of transformativeness.  
64 The various metrics of impact are very closely related to each other. The behavior of our metrics of  
65 transformativeness largely correspond to existing conceptualizations, but provide insights. Conventional  
66 citation measures of impact are related to transformativeness, but our metrics show substantial  
67 independent variations in transformativeness for a given level of impact ( $\rho=.401$ ). Thus, impact and  
68 transformativeness are empirically (as well as conceptually) distinct, each representing distinctive,  
69 cohesive phenomena.

70 Measures of scientific output and creativity in the social science literature rarely extend beyond  
71 publication counts, perhaps weighted by some journal ranking, and citation counts, which do not  
72 adequately distinguish work that is influential within a paradigm from work that is influential and also  
73 path-breaking and therefore do not allow separate analysis of impact and transformativeness in science.  
74 Recent work has sought to address deficiencies of standard citation methods (e.g., Wang, Song, and  
75 Barabasi [2013] and Hutchins, Yuan, Anderson, and Santangelo [2015]). Acemoglu, Akcigit, and Celik  
76 [2015] use a range of rich characterizations of citations to identify the most innovative work. Wang,  
77 Veugelers, and Stephan (2016) identify novel research from unique combinations of citations. Funk and  
78 Owen-Smith (Forthcoming) uses shifts in citation patterns to identify work that consolidates or  
79 destabilizes existing technologies. Evans and Foster (2016) overview approaches to identifying novelty  
80 and develop a unifying simulation approach.

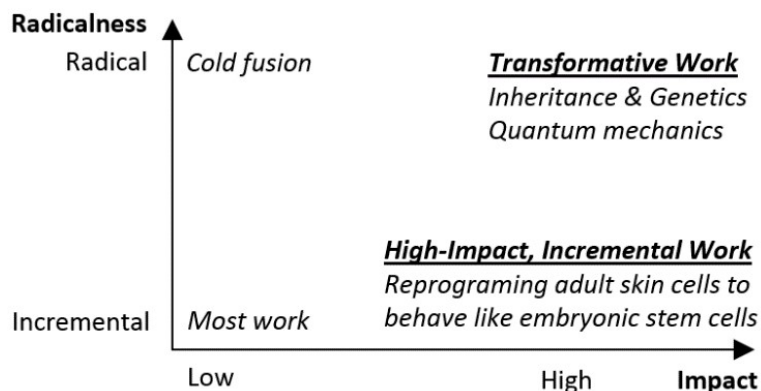
81 Cronin and Sugimoto (2014, 2015) review a wide range of scholarly metrics that are commonly used in  
82 citation and scholarly impact analysis but also in academic auditing. While traditional metrics use a  
83 quantitative analysis of publications, authors, bibliographic references, and related concepts, novel  
84 metrics also take into account text, acknowledgments, endorsements, downloads, recommendations,  
85 blog posts, and tweets. They argue that multi-dimensional metrics—also called mixed indicators—are  
86 most valuable as the performance of a person, institution, or country cannot be adequately measured  
87 by any single indicator. This is in line with research by Bollen et al. (2009) which compared 39 existing  
88 and proposed metrics of scholarly impact that are calculated on the basis of both citation and usage log  
89 data. They performed a principal component analysis of the rankings produced by these metrics to  
90 investigate how the different metrics relate to each other, and how accurately and completely they  
91 express scientific impact. They too conclude that the notion of scientific impact is a multi-dimensional  
92 construct and multiple metrics are needed to cover impact.

93 Research by Hanning et al. (2011) developed and validated mixed indicators that help identify emerging  
94 research areas. Bettencourt, Kaiser, and Kaur (2009) use the evolution of scientific collaboration  
95 networks to trace the evolution of fields. The work presented in this paper is novel as it focuses on the  
96 development of metrics that support the identification of high-impact and transformative science (HITS).

## 97 2. Conceptualization of Transformative Work

98 Consistent with NSB (2007), scientific works vary continuously along two dimensions: 1) the extent to  
99 which they are radical (versus incremental) and 2) their impact, from low to high. These dimensions are  
100 illustrated in Figure 1. Most work in science is incremental, increasing knowledge and practices within an

101 established paradigm or theoretical framework. As knowledge, products, and practices accumulate  
 102 incrementally, moderate amounts of knowledge and practices become obsolete. High-impact  
 103 incremental work naturally has a large impact on a field but lies within an existing paradigm.  
 104 Consequently, high-impact, incremental work does not make obsolete a large amount of research  
 105 (relative to its impact). Radical work differs from incremental work in that it represents a break from an  
 106 existing paradigm. The highest-impact radical work is transformative and game-changing, fundamentally  
 107 altering a discipline, making existing theories, paradigms, and knowledge obsolete, or at least less  
 108 salient. It also generates new research opportunities, potentially across many fields. Of course, not all  
 109 radical work has a high impact. Low-impact radical work neither contributes to an established paradigm  
 110 nor successfully replaces one. Our distinction between incremental and radical work parallels Kuhn's  
 111 (1947) distinction between normal and revolutionary science. We hypothesize that this classification  
 112 applies to non-scientific innovation and across research motivations (as in Stokes [1997]).



113  
 114 **Figure 1.** Classification of scientific work by radicalness and impact, with examples.

115 Figure 1 provides examples that illustrate our classification, although we caution that a rigorous  
 116 classification requires formal metrics such as those proposed in this paper.

117 Lower-left quadrant: Most scientific work is incremental and has a comparatively low impact. For  
 118 example, in genetics and related fields, the discovery that two genes interact to produce a particular  
 119 phenotype often is a publishable result. Dissecting the molecular mechanism controlling gene  
 120 expression, however, is a more difficult and significant advance; this is the type of finding that is  
 121 published in the top journals in molecular biology and genetics, such as *Cell*, and that has a higher  
 122 impact.

123 Lower-right quadrant: According to *Time Magazine*, one of the top-ten scientific discoveries of 2007 was  
 124 a method to reprogram skin cells to behave like embryonic stem cells. This discovery is likely to have a  
 125 high impact because it provides a means to obtain stem cells without destroying human embryos, thus  
 126 bypassing legal and ethical roadblocks to stem cell research. From a clinical perspective, it offers the  
 127 potential of regenerating from a punch of skin a patient's pancreas, liver, muscle, and so forth that are  
 128 exactly like the patient's own. This method is credited to two research teams working independently,  
 129 each publishing its findings in November 2007. As of July 2016, according to Google Scholar, these two  
 130 articles received 7,752 and 11,707 citations, respectively. Despite its high impact, this discovery did not  
 131 radically alter a scientific paradigm. We therefore place this advance high on the impact scale but low on  
 132 the radicalness scale.

133 Top-right quadrant: Quantum mechanics is a canonical example of transformative work in the 20th  
 134 century, as it marked a shift from classical physics, changed physicists' view of the world, and impacted

135 other fields, such as chemistry. Examples of transformative research in biomedicine range from a series  
136 of breakthroughs in genetics and inheritance from Mendel’s genetic theory, to the discovery of the link  
137 between the DNA and inheritance, to the identification of the structure of DNA, which launched the  
138 fields of genetics and molecular genetics.

139 Top-left quadrant: Low-impact radical works are works that fail or lead to dead ends (e.g., cold fusion;  
140 see Bettencourt, Kaiser, and Kaur [2009]) and radical works that impact a small area or make a small  
141 advance to a paradigm.

142 Scientific contributions can be classified as “conceptual” (e.g., discovery of the DNA structure) or  
143 “technical,” involving the development of methods or tools. Our classification of scientific works applies  
144 to both. Insofar as a technical contribution incrementally improves existing techniques and does not  
145 radically alter practices or overturn the theoretical framework, paradigm, or body of knowledge, it will  
146 be incremental. A new tool or method that renders existing tools or methods obsolete or whose  
147 application directly changes the theoretical paradigm in use is transformative. The invention of the  
148 tunneling microscope was transformative because it enabled new inquiries that ultimately resolved  
149 longstanding, fundamental questions and created new bodies of knowledge and even new fields (Chen,  
150 2007). Another example of a transformative scientific discovery of a technical nature is the discovery in  
151 1998 of RNA interference (RNAi), a natural process by which cells silence the activity of specific genes.  
152 Prior to the discovery of RNAi, nearly the only method available to disable a gene in mammals was by  
153 creating knockout or transgenic animal models, a very time-intensive and uncertain process. RNAi-  
154 based gene suppression is now the state-of-the-art method by which scientists can “knock down”  
155 specific genes in cells to learn about gene function (Gao and Zhang, 2007).

156 As indicated, in seeking to develop HITS metrics, we draw on existing conceptualizations from NIH, NSF,  
157 and the NSB. In recent years, the NIH has established programs that specifically target transformative  
158 research. The objective of NIH’s Roadmap Transformative Research Projects Program (R01) is to support  
159 “exceptionally innovative and/or unconventional research projects with the potential to create or  
160 overturn fundamental paradigms. These projects tend to be inherently risky and may not fare well in  
161 conventional NIH review... The primary emphasis of the Transformative Research Award is to support  
162 research on bold, paradigm-shifting but untested ideas” (NIH, 2015). The Common Fund's NIH Director’s  
163 Transformative Research Award is intended to “support research on bold, paradigm-shifting but  
164 untested ideas” (NIH, 2015). The NSF defines transformative research as involving “ideas, discoveries, or  
165 tools that radically change our understanding of an important existing scientific or engineering concept  
166 or educational practice or leads to the creation of a new paradigm or field of science, engineering, or  
167 education. Such research challenges current understanding or provides pathways to new frontiers (NSF,  
168 2015)”. It describes transformative research as “revolutionizing entire disciplines; creating entirely new  
169 fields; or disrupting accepted theories and perspectives—in other words, those endeavors which have  
170 the potential to change the way we address challenges in science, engineering, and innovation.”  
171 Because potentially transformative research challenges the research agendas of experts on review  
172 panels, it may not receive a fair hearing. Also as the NSB notes, transformative research frequently  
173 crosses disciplinary lines adding to the challenge of evaluating the work. Nonetheless it views  
174 transformative research as being “of critical importance in the fast-paced, science and technology-  
175 intensive world of the 21st Century (NSB, 2007)” and thus should be of paramount importance in  
176 determining how scarce funding is allocated.

177 These descriptions point to seven aspects of transformative work, many of which appear in multiple  
178 conceptualizations, and are often described using the same vocabulary. Given the lack of formal metrics  
179 for transformative work, we view these aspects as potentially characterizing transformative work, with

180 the actual features of transformative work being an empirical question that we seek to address in this  
181 work. The characteristics and how they map back to the conceptualizations, are outlined in Appendix A,  
182 Table A.1, and described in detail below. All metrics for transformative work are computed at the level  
183 of field-period pairs as motivated in Section 3. The seven characteristics of transformative work and the  
184 metrics we develop to measure them are:

- 185       **(1) Radical-Generative**—Transformative research is viewed as critical because it generates radical  
186 new paradigms, theories, perspectives, and fields. We measure the generative aspect of  
187 transformative research using the introduction of heavily used new terms, measured by a metric  
188 called *Concepts*, and the utilization of important new terms, called *BMentN*, where N indicates  
189 the number of years (0, 3, 5, 10,  $\infty$ ) since the term was first used in an article. (Here and  
190 elsewhere, “B” and “F” prefixes indicate backward and forward measures; “Ment” indicates  
191 mentions of concepts, “Cite” indicates citations; and “Herf” and “Age” indicate Herfindahl  
192 measures of dispersion and ages.)
- 193       **(2) Radical-Destructive**—In creating radical new paradigms, transformative research is seen to  
194 render large portions of existing knowledge obsolete (or at least less salient). Backward  
195 citations, captured by a metric called *BCiteAge*, indicate the extent to which current research  
196 draws on prior work. Jones and Weinberg (2011) show that backward citations ages contract  
197 during scientific revolutions.
- 198       **(3) Risky**—Because it represents a substantial departure from existing work, the existing  
199 conceptualizations view transformative work as risky. The risky nature is one reason why  
200 transformative work might not receive the support that it merits in funding reviews and why it is  
201 especially important to be able to identify and support it. One natural measure of risk is the  
202 variance in forward citations received by the articles published in a field-period pair, here called  
203 *FCiteVar*.<sup>1</sup>
- 204       **(4) Multidisciplinary**—Transformative work is viewed as more likely to draw on knowledge from  
205 many fields. We use Herfindahl indices (a standard measure of dispersion used by economists)  
206 to measure the breadth of fields that are cited in articles and call this metric *BHerfCite*. In  
207 addition, we generate metrics for the breadth of important new terms that the articles in a field-  
208 period pair draw on. Specifically, we define *BHerfMentN*, where N indicates the number of years  
209 (0, 3, 5, 10,  $\infty$ ) since the term was first introduced into the literature.
- 210       **(5) Wide Impact**—Just as transformative work is viewed as more likely to draw on a wide range of  
211 knowledge, it is seen to be more likely to have a wide impact. We measure the breadth of  
212 impact using Herfindahl indices of the range of fields that cite articles (using a metric we call  
213 *FHerfCite*) and the range of fields that use the terms introduced by articles (using a metric called  
214 *FHerfMent*).
- 215       **(6) Growing Impact**—Because it is radical, the impact of transformative work is seen to take a while  
216 to accumulate. We measure the time path of utilization of transformative work using the mean  
217 time elapsed between when an article is published and the forward citations it receives and call  
218 the corresponding metric *FCiteAge*.
- 219       **(7) High impact**—In order for a radical work to be transformative, it must be high impact, so we  
220 view this aspect of transformative work as somewhat definitional. Put differently, works that are  
221 as radical as transformative work, but that do not have the same impact will not transform  
222 fields. We define the metric *FCiteMean* as the mean forward citation count and the percentiles

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<sup>1</sup> In addition to the riskiness of research in a field-period pair, this measure reflects differences in the importance of work done in a field stemming from other sources.

223 of the distribution of forward citation counts as  $FCiteN$ , where N indicates the percentile of the  
 224 citation distribution (25, 50, 75, 90, 95, 99, 99.9, 99.99).

### 225 3. Data Acquisition and Preparation

226 Two datasets are used to construct and exemplify the eleven metrics: 1) MEDLINE® 2014 baseline files  
 227 distributed by the National Library of Medicine (NLM) containing 22,376,811 articles published between  
 228 1809 and 2014 and 2) 15,085,762 articles from Thomson Reuters’ Science Citation Index Expanded™  
 229 published between 1950 and May 20, 2014, the day our data was acquired. After taking the intersection  
 230 of the two data sources, we are left with 13,737,835 articles published between 1950 and 2014. See  
 231 Table 1 for details.

232 **Table 1: Article Counts**

Data Source	Articles	With Restrictions
MEDLINE 2014 Baseline <i>Published 1809-2014</i>	22,376,811	20,667,693*
Web of Science <i>Published 1950-May 20, 2014</i>	15,085,762	15,080,131**
Intersection		13,737,835
Published 1983-2012		10,778,696

\*There are three restrictions on articles in the MEDLINE data: 1) the article must be the first version of an article, 2) the article must have “MEDLINE” status, and 3) the article must be tagged with at least one 4-digit MeSH term. For details on the version and status of MEDLINE articles (NLM, 2016). For details on 4-digit MeSH terms see below description and Appendix C.

\*\*There is one restriction on articles in the Web of Science (WOS) data: A small number of our WOS records map to a PMID to which other WOS records map. We retain the earliest WOS ID that maps to each PMID, reducing our WOS articles by 5,631 or .037% of our 15,085,762 WOS records.

### 233 Period Identification

234 We are interested in generating two sets of metrics—one based on text analysis and another based on  
 235 citations patterns. Since article abstracts are important for generating our text-based metrics, and  
 236 MEDLINE’s coverage of abstracts is poor before 1980, we limit our sample to articles published in 1983  
 237 or later. Since citations take time to accumulate and our data ends in 2014, we limit our sample to  
 238 articles published in 2012 or earlier. As seen in Table 1, restricting our sample to articles published  
 239 between 1983 and 2012 leaves us with 10,778,696 articles with which to compute our metrics.

### 240 Field Identification

241 The 10,778,696 articles in our analysis sample are tagged with Medical Subject Headings (MeSH) that  
 242 describe the content of the articles. We use these to assign articles to particular fields. There are 27,149  
 243 raw terms in the 2014 MeSH vocabulary and they vary widely in their descriptive detail. For instance,  
 244 some articles are tagged with general terms such as "Body Regions" and some are tagged with more  
 245 detailed terms such as "Peritoneal Stomata". In order to construct comparable fields, we aggregate all

246 MeSH terms to a similar level of descriptive detail. This process—described in detail below and in  
247 Appendix C—leaves us with 6,159 aggregated MeSH terms.

248 To understand our aggregation method, first note that MeSH terms have a hierarchical structure. At the  
249 top of the hierarchy (1-digit terms) are 16 very general terms such as "Anatomy", "Organisms", and  
250 "Diseases". Beneath each of these 1-digit MeSH terms is a group of more detailed 2-digit MeSH terms.  
251 For instance, "Body Regions" is a 2-digit MeSH term beneath the 1-digit term "Anatomy". Beneath each  
252 2-digit MeSH term is a group of even more detailed 3-digit MeSH terms. This structure continues to 12-  
253 digit MeSH terms. To reduce the amount of variation in the breadth of fields, we aggregate all MeSH  
254 terms to the 4-digit level. Aggregation is complicated by the fact that some more detailed (lower level)  
255 MeSH terms are associated with more than one higher-level 4-digit MeSH term. In these cases, we  
256 distribute (prorate) the weight of each higher-level MeSH term evenly across all of the 4-digit MeSH  
257 terms that are beneath it.

258 Once we have finished this aggregation process, we are able to transform each article's raw MeSH  
259 terms, which vary dramatically in terms of degree of aggregation, into 4-digit MeSH terms, which are  
260 considerably more uniform in terms of degree of aggregation. We then characterize the fields to which  
261 an article belongs by prorating the article equally across its 4-digit MeSH terms. Thus, each article is  
262 fractionally assigned to one or more 4-digit MeSH term fields. Appendix C, Figures C.1 and C.2 shows  
263 the distribution of the number of MeSH4 terms per article by publication year.

#### 264 Field-Period Pairs

265 All metrics for high impact and transformative science (HITS) are defined for field-period pairs, i.e., a  
266 combination of a specific 5-year period and 4-digit MeSH term. The span of analysis, from 1983 through  
267 2012, is divided into six consecutive 5-year periods, starting with 1983-1987 and ending with 2008-2012.  
268 Papers are sorted into these bins based on publication year. For each period, there exist 6,159  
269 aggregated 4-digit MeSH terms. Six periods by 6,159 fields results in 36,954 period-field pairs, However,  
270 not all field-period pairs that have articles to generate values for all eleven metrics. Overall, 15,051 field-  
271 period pairs have articles and are used in this study. Table 2 shows the use (mentions) of highly used  
272 concepts (*BMentAll*) and the mean of forward citations (FCiteMean) for five relatively highly ranked  
273 fields. Gene Expression Profiling does not have any articles in two of the periods, but has the highest  
274 value for of *BMentAll* in the 2008-2012 period across the fields displayed. It is noteworthy that *BMentAll*  
275 increases over time because the number of concepts increases while FCiteMean declines in the latest  
276 years because the length of time over which citations can accrue is shorter, a factor we control below.

277



	1983- 1987	1988- 1992	1993- 1997	1998- 2002	2003- 2007	2008- 2012
<b>Field</b>						
<b><i>BMentAll</i></b>						
Gene Expression Profiling	1.00	.	.	4.98	6.22	6.73
Intracellular Signaling Peptides and Proteins	1.03	1.52	3.71	5.89	6.65	6.67
Neoplasm Proteins	1.12	1.75	3.06	4.41	5.38	5.46
RNA Viruses	1.13	1.99	2.69	3.33	3.67	3.73
Retroviridae Infections	1.36	2.60	3.12	4.06	4.61	4.85
<b><i>FCiteMean</i></b>						
Gene Expression Profiling	17.16	.	.	71.25	40.43	16.23
Intracellular Signaling Peptides and Proteins	43.22	65.07	92.85	67.18	40.01	15.89
Neoplasm Proteins	68.62	80.59	78.38	58.96	40.69	15.97
RNA Viruses	35.87	38.10	35.61	35.54	28.44	12.53
Retroviridae Infections	34.69	24.07	22.01	24.29	19.27	9.77

279

280 **Table 2:** Exemplary depiction of field-period pairs. All six time periods are shown but only five of the  
281 6,159 fields.

## 282 4. Methods

283 Eleven metrics grouped by seven different dimensions of impact and transformativeness were  
284 introduced in Section 2 and they are defined and operationalized here.

285 For both the text-based and the citation-based metrics, we develop metrics to identify the impact and  
286 transformativeness of the articles published in a given field-period pair and refer to the articles, fields,  
287 and time periods for which we are measuring impact and transformativeness as the “target” articles,  
288 fields, and time periods. We refer to the articles, fields, and time periods over which we measure the  
289 impact and transformativeness of the target articles as the “measurement” articles, fields, and time  
290 periods. We note that depending on the metric, the measurement period may be before or after the  
291 target period—some of our metrics are forward looking while others are backward looking. Additionally,  
292 our measurement period and target period and field can overlap. Consider an article published in 1990.  
293 That article falls in the 1988-1992 target period. When we count forward citations to that article, we use  
294 citations occurring in articles published from 1990-2014, which includes three years of the 1988-1992  
295 period. Similarly, when we generate backward citation ages for that article, we will get citations to  
296 articles in 1990 and all earlier years, which also includes three years of the 1988-1992 period.

297 To compute the text-based metrics, we begin with the full MEDLINE 2014 baseline files containing  
298 22,376,811 articles published between 1809 and 2014. We index all words, word-pairs, and word-  
299 triplets that appear in the title or abstract of a MEDLINE article. We generically refer to these n-grams as  
300 “concepts”. Next, we extensively process these concepts by eliminating stop words, stemming and  
301 lemmatizing each word, and applying a variety of other operations. See Appendix B for details.

302 After processing the MEDLINE corpus, we take the intersection of the MEDLINE and WOS database  
303 obtaining the 13,737,835 articles in Table 1. This set of articles contains 109,912,224 unique concepts.  
304 Next, we use article publication dates to identify the first year each concept is mentioned. We call this a  
305 concept's "vintage year". Further restricting our sample to the 10,778,696 articles published between  
306 1983 and 2012, we obtain 95,393,331 concepts with vintage years between 1982 and 2012. Next, we  
307 count the number of times a concept is mentioned subsequent to its vintage year. To focus on the most  
308 important concepts, we identify the top .01 percent of concepts from each vintage (including all tied  
309 concepts in the case of ties at the threshold) — a total of 10,128 top concepts (including 589 due to ties)  
310 with vintages between 1983 and 2012. We use these top concepts to construct our text-based metrics.

311 Next, we verbally define each of the eleven metrics we have developed to capture high impact and  
312 transformative work. The full name of each metric and its variable name (in parentheses and italics) as  
313 well as formal definitions are given in Appendix D, Table D1. Summary statistics for all metrics, and all  
314 field-period pairs are presented in Table 3. This table also provides details on the number of field-period  
315 pairs for which each metric can be computed and info on which target periods and fields are associated  
316 with each of the metrics.

### 317 **Radical–Generating**

318 Top Concept Births (*Concepts*): To measure the generation of important new ideas, we measure how  
319 many of the top 10,128 concepts identified in the previous section are produced by a MeSH4 field in a  
320 particular period. To construct this metric, we first assign each concept to a period on the basis of its  
321 vintage. For instance, all concepts with a vintage between 2003 and 2007 are assigned to the 2003-2007  
322 period. Second, we assign each concept to MeSH4 fields. To do this, we identify all articles that use a  
323 particular concept in the first year it was introduced (its vintage year) and then identify the MeSH4 fields  
324 of these articles. We then prorate the concept equally across these fields. Finally, we sum the number of  
325 top concepts assigned to each MeSH4 field-period pair. We call this sum the number of "top concept  
326 births". *Concepts are expected to be increasing with the radicalness of work.*

327 Top Concept Mentions (*BMentN*): To measure the utilization of important new concepts, we identify  
328 how many times one of the top 10,128 concepts identified in the previous section are used within N  
329 (N=0, 3, 5, 10, and all prior years) years of the concept's vintage. To construct this metric, we first  
330 identify all articles that use a top concept from any vintage. Second, we assign each article to a period  
331 on the basis of its publication year. For instance, all articles published between 1993 and 1997 are  
332 assigned to the 1993-1997--period pair. Third, we assign each article to MeSH4 fields by equally  
333 prorating the article across the fields with which the article is tagged. Fourth, we count the number of  
334 top terms introduced within the last N years used by each article. Finally, we sum across all articles  
335 assigned to each MeSH4 field-period pair. We call this sum the number of "top concept mentions".  
336 *BMentN are expected to be increasing with the radicalness of work.*

### 337 **Radical–Destroying**

338 Backward Citation Age (*BCiteAge*): This measure reflects the age of the works cited in articles. The age of  
339 a backward citation is the difference between the publication year of the citing article and the  
340 publication year of the cited article (backward citation). For each citing article, a mean backward  
341 citation age is constructed by averaging the ages of its backward citations. *BCiteAge* for a target MESH4  
342 field and 5-year period is the average of the average backward citation age across all articles published  
343 in the target field -period pair. *BCiteAge decreases with destructive radicalness.*

### 344 **Risky**

345 Variance of Forward Citations (*FCiteVar*): In economics, the variance of the returns to an investment or  
 346 asset are used as a proxy for the investment or asset's risk. Here the risky nature of articles published in  
 347 a field-period pair is measured by the variance in forward citations they receive. This metric uses all  
 348 subsequent years (including later years in the target vintage) without limitations. For example, suppose  
 349 a target field-period contains three articles, each assigned exclusively to the target field. Now consider  
 350 one case in which each article receives 30 citations, and a second case in which two articles receive no  
 351 citations and one receives 90 citations. The field-period forward citation mean is the same in both cases  
 352 (it is 30) but in the first case *FCiteVar* is 0  $\left(= \frac{1}{3}(3 \times (30 - 30)^2)\right)$  and in the second case *FCiteVar* is  
 353 1800  $\left(= \frac{1}{3}(2 \times (0 - 30)^2 + (90 - 30)^2)\right)$ . *FCiteVar ranges between 0 and infinity and increases with*  
 354 *riskiness.*

### 355 **Multidisciplinarity**

356 Herfindahl of Backward Citations (*BHerfCite*): *BHerfCite* for a target MeSH4 field and 5-year period is an  
 357 index of field dispersion of the articles cited by the articles published in that target field and period.  
 358 *BHerfCite* is computed by squaring the total number of backward citations from each field, summing  
 359 over the squares, and subtracting the result from 1. For example, if the articles published in a target  
 360 field-period cited 1500 articles, 500 in each of three fields, the field-period's *BHerfCite* would be .667 ( $=$   
 361  $1 - \left(\frac{1^2}{3} + \frac{1^2}{3} + \frac{1^2}{3}\right)$ ). *BHerfCite ranges between 0 and 1 and increases with multidisciplinarity—the*  
 362 *breadth of fields from which the article draws.*

363 Herfindahl Index of the Breadth of Existing Concepts Used (*BHerfMentN*): To measure the breadth of  
 364 ideas that a field is drawing on, we use a Herfindahl index of the dispersion of the top concepts used by  
 365 the articles published in that target field and vintage period. For a set of concepts from a given field and  
 366 vintage period, we square each n-gram's share of total mentions. We then sum over the squares and  
 367 subtract them from 1. We do this separately by the number of years ( $N=0, 3, 5, 10$ , and all prior years)  
 368 since each concept was first used. *BHerfMentN ranges between 0 and 1 and increases with the breadth*  
 369 *of ideas from which the field draws.*

### 370 **Wide Impact**

371 Herfindahl Index of Forward Citations (*FHerfCite*): *FHerfCite* for a target MESH4 field and 5-year period is  
 372 an index of field dispersion of the articles citing the articles published in that target field and vintage.  
 373 *FHerfCite* is computed by squaring the share of forward citations from each field, summing over the  
 374 squares, and subtracting the result from 1. For example, if the articles published in a target field-period  
 375 were cited by 1500 articles, 500 in each of three fields, the field-period's *FHerfCite* would be .667 ( $= 1 -$   
 376  $\left(\frac{1^2}{3} + \frac{1^2}{3} + \frac{1^2}{3}\right)$ ). *FHerfCite ranges between 0 and 1 and increases with breadth of impact.*

377 Herfindahl Index of the Breadth of the Future Use of Concepts Introduced (*FHerfMent*): To measure the  
 378 breadth of use of the concepts generated in a field, we use a Herfindahl index of the dispersion across  
 379 fields in the future use of the concepts introduced in a field-period pair. For a set of concepts from a  
 380 given field and vintage period, we take the share of mentions in subsequent periods across all fields,  
 381 square each field's share of total mentions. We then sum over the squares and subtract them from 1.  
 382 *FHerfMent ranges between 0 and 1 and increases with breadth of use of the concepts generated in a*  
 383 *field.*

### 384 **Growing Impact**

385 Forward Citation Age (FCiteAge): This measure captures the typical length of time between when works  
 386 are published and citations to that work occur. The age of a forward citation to a cited article is the  
 387 difference between the publication year of the citing article (forward citation) and the publication year  
 388 of the cited article. For each cited article, a mean forward citation age is constructed by averaging the  
 389 ages of its forward citations. *FCiteAge* for a target MeSH4 field and 5-year period is the average of the  
 390 article averages of forward citation age across all cited articles published in the target field-period.  
 391 *FCiteAge increases with growth of impact.*

## 392 High Impact

393 Mean Forward Citation Count (FCiteMean): *FCiteMean* for a target MESH4 field and 5-year period is the  
 394 average forward citation counts across all articles (including those that receive no citations) published in  
 395 the target field and period. *FCiteMean increases with impact.*

396 Forward Citation Percentile (FCiteN): This series of metrics captures the impact as measured by forward  
 397 citation counts at various percentiles of the distribution of forward citations. Formally, we rank articles  
 398 in a target field-period pair by their forward citation counts (including those that receive no citations).  
 399 *FCiteN* is the forward citation count below which *N* percent of articles in a target field-period pair are  
 400 found. For example, *FCite75* is the forward citation count of the article at the 75th percentile for the  
 401 target field and period. *FCiteN* is constructed for *N* = 25, 50, 75, 90, 95, 99, 99.9 and 99.99. *FCiteN*  
 402 *captures the impact of the most cited articles in a target field-period and increases with impact.*

403 As indicated, articles may be assigned to more than one MeSH category. In calculating each metric for  
 404 each MeSH category, we weight articles by the share of the article falling in that MeSH category.

405 **Table 3:** Summary Statistics for all Metrics for time periods 1983-1987, ..., 2008-2012 and all MESH4  
 406 Fields in MEDLINE.

Variable Name	Mean	S.D.	Measurement Term and Fields
<b>Citation-Based Metrics</b>			
FCiteMean	22.309	12.670	All subsequent years (including later years in the target vintage) through 2014. All of MEDLINE.
FCite25	3.489	2.656	All subsequent years (including later years in the target vintage) without limitations. No limitations on measurement fields. Includes both MEDLINE and non-MEDLINE indexed articles.
FCite50	9.838	6.137	
FCite75	23.767	13.366	
FCite90	50.264	27.736	
FCite95	78.926	44.069	
FCite99	192.525	111.922	
FCite99.9	586.390	393.483	
FCite99.99	1626.023	1623.863	
FHerfCite	0.979	0.005	All subsequent years (including later years in the target vintage) through 2014. All of MEDLINE.
FCiteAge	5.229	2.555	All subsequent years (including later years in the target vintage) through 2014. All of MEDLINE.
BHerfCite	0.979	0.006	All previous years (including earlier years in the target vintage) without limitations. All of MEDLINE.

BCiteAge	9.642	2.605	All previous years (including earlier years in the target vintage) without limitations. No limitations on measurement fields. Includes both MEDLINE and non-MEDLINE indexed articles.
FCiteVar	4803.615	14596.430	All subsequent years (including later years in the target vintage) without limitations. No limitations on measurement fields. Includes both MEDLINE and non-MEDLINE indexed articles.
<b>Text-Based Metrics</b>			
Concepts	32.235	72.099	1983-1987,..., 2008-2012; All MESH4 Fields in MEDLINE.
BMent0	0.003	0.006	1983-1987,..., 2008-2012; All MESH4 Fields in MEDLINE.
BMent3	0.037	0.033	
BMent5	0.085	0.078	
BMent10	0.294	0.258	
BMentAll	1.028	0.930	
FHerfMentions	0.996	0.008	1983-1987,..., 2008-2012; All MESH4 Fields in MEDLINE.
BHerfMent0	0.910	0.184	All articles that use a concept within N (N=0, 1, 3, 5, all years) years of the concept's vintage and published during the 1983-1987,..., 2008-2012 periods. All MESH4 Fields in MEDLINE.
BHerfMent3	0.969	0.066	
BHerfMent5	0.976	0.053	
BHerfMent10	0.981	0.047	
BHerfMentAll	0.983	0.046	

407 Note. 15,051 Field-Period pairs.

## 408 5. Results: Comparison of Metrics

409 The eleven general metrics were analyzed and compared using a factor analysis to identify different  
410 dimensions of transformativeness. Because the forward citation rates are the conventional measure of  
411 impact or influence, we perform a factor analysis on impact metrics as a group.

412 When conducting the factor analysis, we first compute the natural logarithm of one plus all metrics and  
413 then take deviations from field and period means. We do this by regressing the natural logarithm of one  
414 plus each variable on a set of dummy variables for 4-digit MESH field and a set of dummy variables for 5-  
415 year period. Formally, let  $M_{fp}$  denote the value of a metric for field  $f$  in period  $p$ ;  $\overrightarrow{F_{fp}}$  denote a vector of  
416 field dummy variables (or fixed effects) equal to one for field  $f$  and zero for the other fields; and  $\overrightarrow{P_{fp}}$   
417 denote a vector of period dummy variables (fixed effects) equal to one for period  $p$  and zero otherwise.  
418 We estimate,

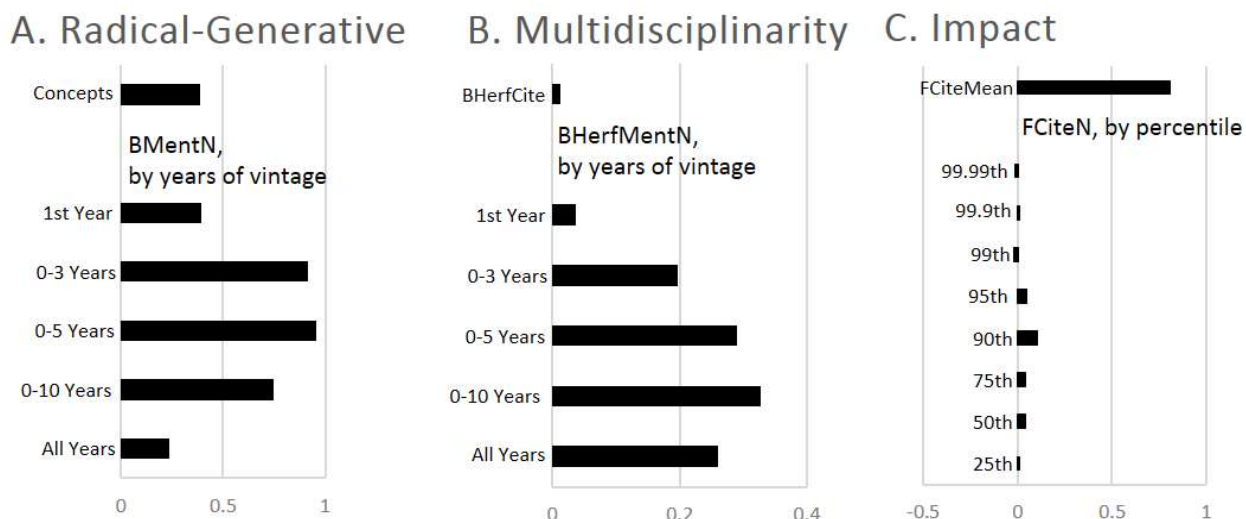
$$419 \ln(M_{fp} + 1) = \overrightarrow{F_{fp}}' \beta + \overrightarrow{P_{fp}}' \gamma + \epsilon_{fp} .$$

420 We analyze the residuals from this equation,  $\epsilon_{fp}$ . Taking the natural logarithm of the metrics reduces  
421 weight on variations in the right tail of the metrics, which tend to be highly right-skewed (adding 1 is a  
422 commonly used approach to address values of zeros). The period dummy variables address the end of  
423 our outcomes data in 2014, with the various vintages being different lengths of time from being

424 truncated. Eliminating such cross-period variation when estimating factor loadings means that changes  
 425 in the overall level of the metrics from period to period do not influence the factor loadings. We run the  
 426 same comparison dropping the 2008-2012 period and found similar results. The field dummy variables  
 427 address differences across fields in characteristics such as size. Thus, large fields are likely to generate  
 428 more citations and the concepts they originate are likely to be more heavily mentioned. Eliminating  
 429 cross-field variation in estimating the factor loadings means that the metrics are not influenced by  
 430 overall differences across fields.

431 For all subsequent analyses, the dataset comprises all 15,051 field-period pairs and observations are  
 432 weighted by the number of articles in that field-period pair.

433 Figure 2 reports results from the factor analysis for the three composite metrics – Radical Generative  
 434 work, which combines *Concepts* and *BMentN*; Multidisciplinarity, which combines *BHerfCite* and  
 435 *BHerfMentN*; and *Impact*, which combines *FCiteMean* and *FCiteN*. Note that the metrics for Radical  
 436 Destructive work (*FCiteAge*), Risky work (*FCiteVar*), and Increasing Impact (*FCiteAge*) are all generated  
 437 from a single metric, so that no factor analysis was performed. The metric for Breadth of Impact is based  
 438 on only 2 metrics (*FHerfCite* and *FHerfMent*) and the factor analysis is not plotted. In all cases, the first  
 439 factor accounts for the vast majority of the variation (79%-94%) and is the focal point here.



440 **Figure 2.** Factor analysis results for three of the seven metrics types. Share of variation explained by first  
 441 factor is .790 for Radical-Generative work.943 for Multidisciplinarity; and .853 for Impact.  
 442

443 Radical-Generative science (Panel A) loads positively on the birth of new concepts (*Concepts*) and the  
 444 mentions of important concepts of various ages (*BMentN*), with the highest loading on concepts that are  
 445 0-5 years old. Thus, concepts that are older receive less weight than those that are 0-5 years old, while  
 446 those that are younger receive more weight because they appear in multiple groups.

447 Multidisciplinary science (Panel B) loads positively on the dispersion of citations (*BHerfCite*) and the  
 448 dispersion in the use of top concepts (*BHerfMentN*), both measured using Herfindahl indices. The  
 449 loading on concepts that are 0-10 years old is the highest, but concepts in their first year since origin is  
 450 the highest because these concepts are included in the other age categories, so the dispersion of the use  
 451 of the newest concepts is particularly related to multidisciplinarity.

452 Our metric for high Impact science (Panel C) is generated from the mean of forward citations  
 453 (*FCiteMean*) and quantiles of the distribution of forward citations *FCiteN* (here constructed for N = 25,  
 454 50, 75, 90, 95, 99, 99.9 and 99.99), which tend to be closely related. The first factor of impact accounts  
 455 for 85% of the variation. Mean Citations (*FCiteMean*) has the highest factor loading. Interestingly, the  
 456 factor loadings on the quantiles of the forward citation distribution increase from the 25<sup>th</sup> percentile of  
 457 the citation distribution through the 90<sup>th</sup> percentile and then decline, so that the lowest factor loadings  
 458 for the 99<sup>th</sup> and the 99.99<sup>th</sup> percentile of the citation distribution are slightly negative (the 99.9<sup>th</sup> is  
 459 positive, but small, .00663). We show below that these papers that are most likely to be transformative.

460 Table 4 reports correlations between the various aspects of impact and transformativeness. The results  
 461 show that many aspects of transformativeness are positively correlated, indicating some real cohesion  
 462 of these metrics of transformativeness. The Radical-Generative and Risky metrics are comparatively  
 463 highly correlated ( $\rho=.271$ ), suggesting that they are capturing inter-related phenomena. Both metrics  
 464 are strongly positively correlated with High Impact ( $\rho=.383$  and  $.556$ , respectively). Multidisciplinarity  
 465 and Wide Impact research are also comparatively highly correlated ( $\rho=.246$ ). It is intuitive and reassuring  
 466 that work that draws on a wide range of work itself draws on by a wide range of work.

467 Other aspects of transformativeness appear to be only weakly related or unrelated. Radical-Generative  
 468 is essentially uncorrelated with Wide Impact across disciplines ( $\rho=.067$ ). Radical-Destructive is only  
 469 weakly correlated with Radical-Generative ( $\rho=.105$ ) suggesting that the generation of important new  
 470 concepts in a field frequently occurs without rendering old science obsolete. Radical-Destructive is  
 471 essentially uncorrelated with Risky ( $\rho=.050$ ) and Wide Impact ( $\rho=-.017$ ), but weakly negatively correlated  
 472 with Multidisciplinarity ( $\rho=-.096$ ). Interestingly, Multidisciplinarity is also not strongly correlated with  
 473 High Impact ( $\rho=.100$ ) or Radical-Generative ( $\rho=-.076$ ). These correlations contrast with the perspective  
 474 that work that brings together differing scientific approaches or viewpoints generates more influential  
 475 and radical scientific output.

476 **Table 4.** Correlations between individual metrics of Impact (labeled “Impact”) and Transformativeness  
 477 (the other six metrics).

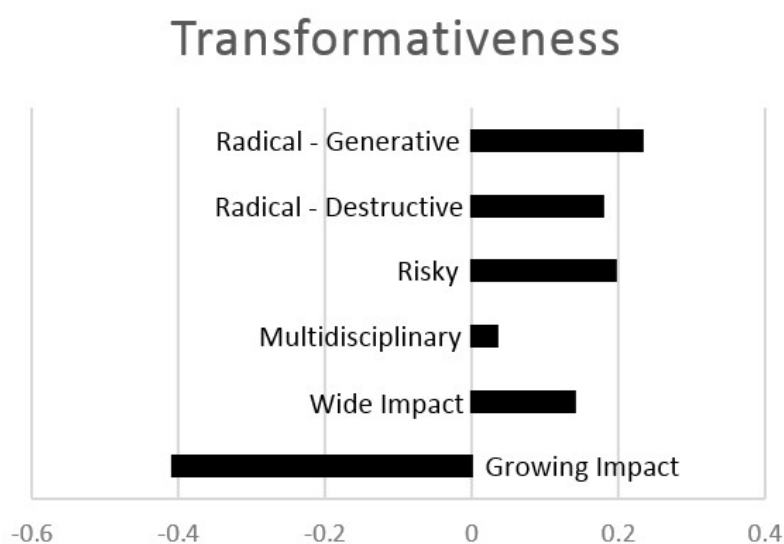
	Radical - Generative	Radical - Destructive	Risky	Multidis- ciplinary	Wide Impact	Growing Impact	High Impact
Radical - Generative	1						
Radical - Destructive	0.1047	1					
Riskiness	0.2714	0.05	1				
Multi-Disciplinarity	-0.0756	-0.0961	0.0764	1			
Wide Impact	0.0672	-0.0167	0.0841	0.2467	1		
Growing Impact	-0.2941	-0.3528	-0.2318	-0.0348	-0.2424	1	
Impact	0.3832	0.0271	0.5561	0.0999	0.0342	-0.1995	1

478  
 479 The strongest correlation observed in Table 4 is between High Impact and Risky ( $\rho=.556$ ). We see a  
 480 strong correlation between the variance in forward citation counts and citations at *all* quantiles of the

481 citation distribution, including the 25<sup>th</sup> percentile and the median, for example. This suggests the  
482 possibility of a trade-off between risk and return in scientific research.

483 As indicated, growth of impact over time, measured by the average time to citations, is negatively  
484 correlated with all the other metrics, which contrasts with views that transformative work takes a long  
485 time to have an impact. We have broken forward citations to the work in each field-period pair into  
486 those arising in the first five years since publication and those arising six or more years since publication.  
487 Both metrics are positively related to each aspect of impact and transformativeness, but citations in the  
488 first 5 years are more strongly correlated with the other metrics for transformativeness (and impact)  
489 than are citations six or more years out - the correlation between transformativeness and citations in  
490 the first five years is .674 while that between transformativeness and citations six or more years after  
491 publication is only .247. Put differently, transformative work is heavily cited in the long run, but it is even  
492 more heavily cited in the short run. A limitation of the study is that we cannot measure impact over very  
493 long time periods, thus we cannot rule out the possibility that the most transformative work grows in  
494 impact over much longer time horizons, e.g. over many decades.

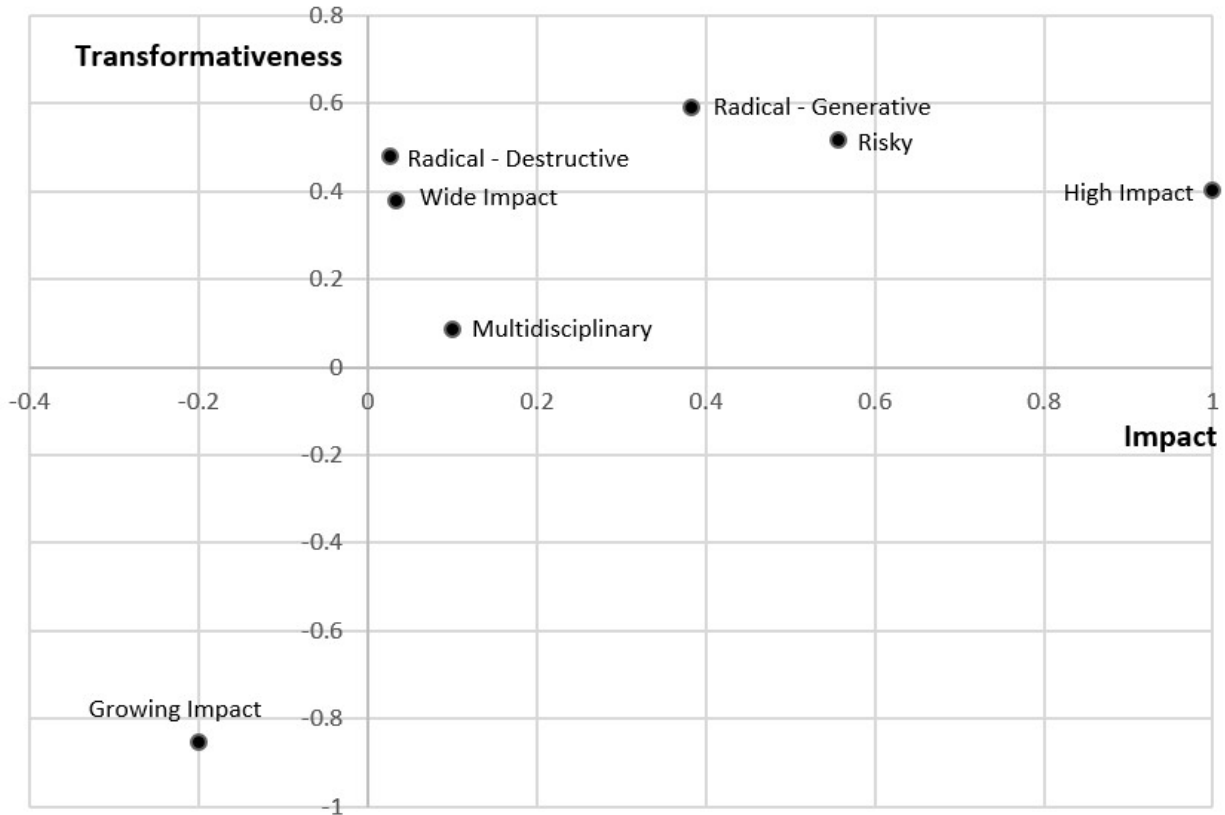
495 Figure 3 shows the first factor from a factor analysis of the six metrics of transformativeness (which  
496 accounts for 107% of the variation). High Impact was excluded to assess how impact and  
497 transformativeness are related. Transformativeness loads positively on all of the metrics but Growing  
498 Impact, suggesting that transformativeness represents a cohesive construct.



499  
500 **Figure 3.** Factor analysis of six different HITS metrics, High Impact is omitted.

501 Figure 4 relates the seven HITS metrics to impact and transformativeness. Aside from Growing Impact,  
502 all the metrics of transformativeness are positively related to both impact and transformativeness. The  
503 metric for High Impact has a correlation with itself of 1 (by construction) and a correlation with  
504 transformativeness of .401. Thus, while impact and transformativeness are positively related, they also  
505 seem to constitute distinct phenomena. The Risky metric is most strongly correlated with Impact.  
506 Radical-Destructive and Wide Impact are both strongly related to transformativeness, but essentially  
507 unrelated to impact. Lastly, Growing Impact is strongly negatively related to transformativeness and  
508 somewhat negatively related to Impact. Interestingly, the correlation between impact and citations in  
509 the first five years is .881, falling slightly to .762 for citations six or more years after publication.

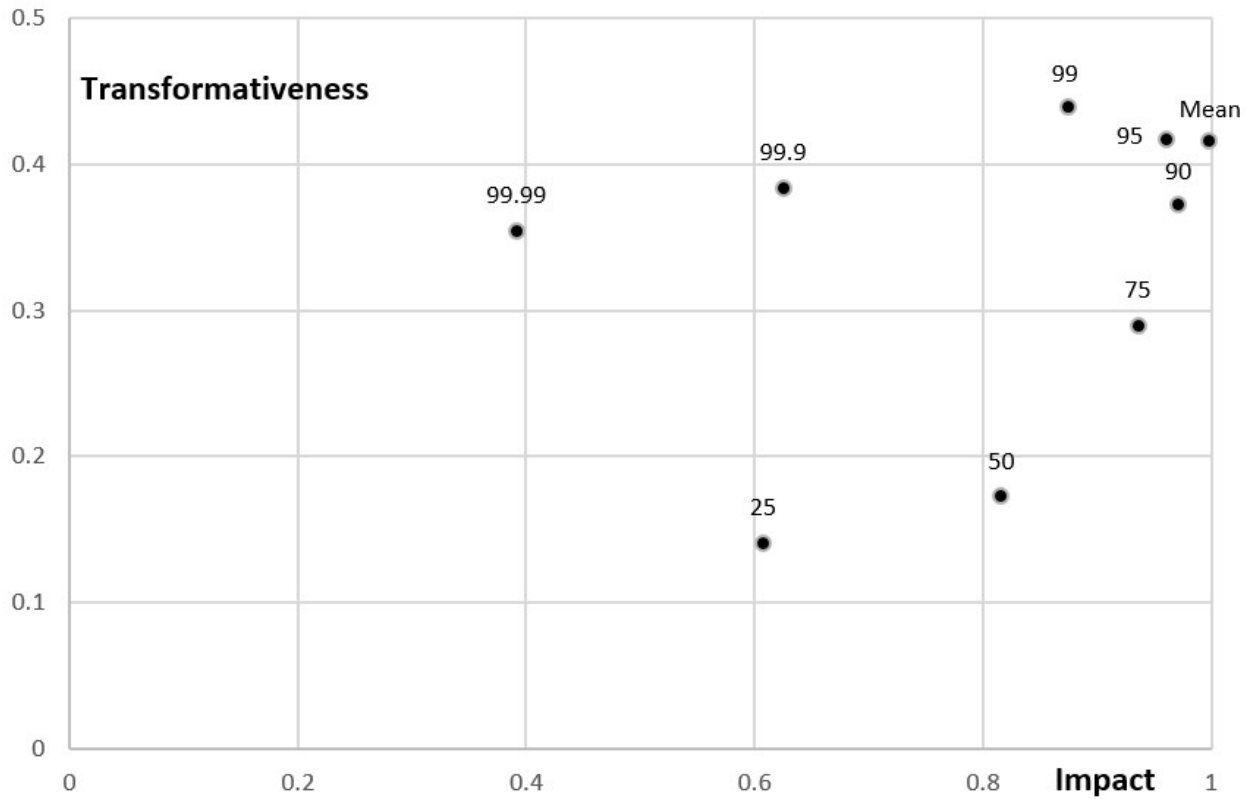




510

511 **Figure 4.** All seven HITS metrics related to Impact and Transformativeness

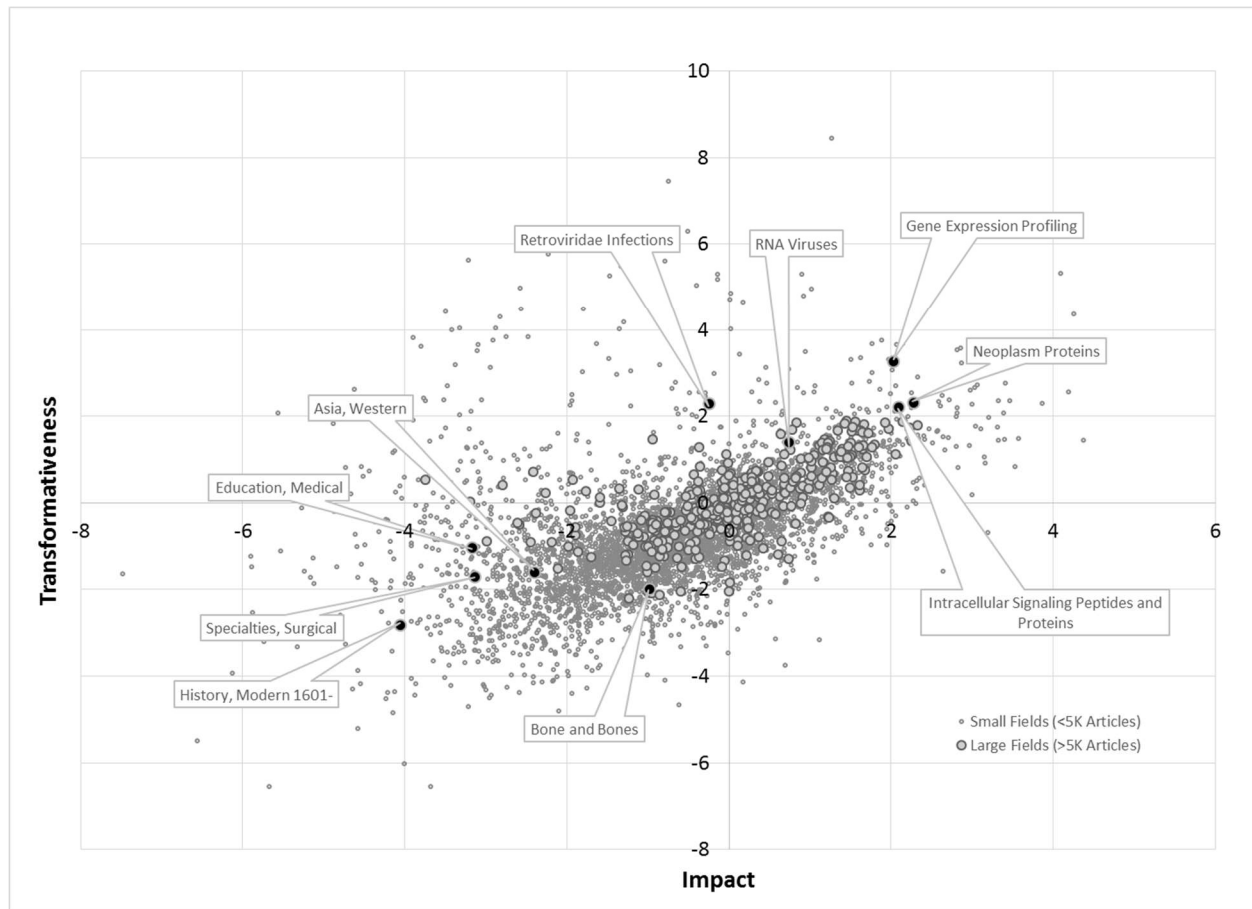
512 Figure 5 shows how the various forward citation metrics (*FCiteMean* and *FCiteN*) relate to impact and  
 513 transformativeness. As indicated in Figure 2C, impact loads most heavily on mean citations and citations  
 514 at the 90<sup>th</sup> percentile with weight declining (or going negative) at the highest and lowest percentiles of  
 515 the citation distribution. The correlations between the impact measure and the highest percentiles of  
 516 the citation distribution are positive even though the factor loadings are negative because all of the  
 517 citation metrics are positively correlated. It is intuitive that transformative works should be  
 518 exceptionally highly cited. Indeed, the strength of the relationship between the percentiles of the  
 519 citation distribution and transformativeness increase monotonically up to the 99<sup>th</sup> percentile of the  
 520 citation distribution (compared to the 90<sup>th</sup> percentile for citations) and then decline moderately to the  
 521 99.99<sup>th</sup> percentile. Strikingly the 99.99<sup>th</sup> quantile of the citation distribution is almost as strongly related  
 522 to transformativeness as it is to impact. These results suggest that the most cited impactful works reflect  
 523 a distinct phenomenon from other high impact work and that they are the most likely to be  
 524 transformative.



525

526 **Figure 5.** FCiteN related to Impact and Transformativeness

527 To provide some summary of our analysis, we take the factor loadings from our factor analysis and use  
 528 them to generate the impact and transformativeness metrics for each 4-digit MESH fields, see Figure 6.  
 529 In doing so, we average across all of the periods from 1982-2012. While there are differences across  
 530 fields, we do not eliminate field differences for this analysis. The figure shows a strong positive  
 531 relationship between impact and transformativeness, but also differences. For instance, gene and  
 532 expression profiling, retroviridae infections, and RNA viruses all score considerably higher on  
 533 transformativeness relative to impact. Interestingly, there are many low impact fields and fields that are  
 534 also rather low in transformativeness. Many relate to historic or societal factors rather than to  
 535 biomedical conditions, treatments or technologies.



537

538 **Figure 6.** Ranking of fields in terms of impact and transformativeness across all periods (1982-2012).  
 539 Field size determined by the number of (weighted) articles across all periods.

540 Just as we preserve the cross-field variation in estimating the field rankings, we have rerun the factor  
 541 analysis preserving the cross-field variation. The results are broadly similar to those reported above,  
 542 with all the components of transformativeness entering in the same way as above. One clear difference  
 543 is that the correlation between transformativeness and impact is higher when cross-field variation is  
 544 preserved ( $\rho=.668$  versus  $.401$ , when the cross-field variation is eliminated). This result is intuitive, in  
 545 that it indicates that differences in transformativeness across fields are more strongly related to impact  
 546 than are changes in transformativeness within fields over time. Put somewhat differently, the fields that  
 547 are transformative tend to be more impactful while fields that are temporarily more transformative  
 548 experience smaller increases in impact.

## 549 6. Discussion

550 The science policy community is increasingly focusing on transformative research, yet there are few  
 551 metrics to identify it and, ironically, the related concept of revolutionary science is falling out of favor.  
 552 Drawing on existing conceptualizations of transformative research, this paper presented eleven metrics  
 553 of transformative research. Specifically, transformative research is viewed as being radical, both

554 generating important new ideas and destroying existing ideas; multidisciplinary and impacting a wide  
555 range of disciplines; risky; having a wide and growing impact over time; and having a high impact.

556 The metrics were exemplarily applied to 15,051 fields of biomedical research over six five-year periods  
557 from 1983-1987 to 1988-2012. Our validation studies show that the metrics behave as expected.  
558 Transformativeness and impact are positively correlated ( $\rho=.401$ ), but distinct. The interrelations  
559 between specific metrics of transformativeness are often positively related but some are only weakly  
560 related or unrelated. Metrics of the use of wide-ranging ideas or multidisciplinary are closely related to  
561 the breadth of impact. A notable exception we find is that the growth of citations is negatively related to  
562 transformativeness—while citations six or more years after publication are increasing in  
563 transformativeness, citations within the first five years increase even more. Whether this represents the  
564 limitations of the timespan of our data or a fundamental fact of transformative research, we leave to  
565 future research. In addition, we find that the displacement of old science coincides with the generation  
566 of radical new science only moderately, and that neither correlates strongly with multidisciplinary.  
567 Interestingly we find a strong positive association between impact and riskiness which suggests the  
568 possibility a trade-off between risk and return in scientific research.

569 Decision makers have a number of choices when selecting metrics, with individual choices depending on  
570 data access, preferences, but also expertise and computational resources. All metrics for MEDLINE  
571 articles introduced in this paper are freely available for scholarly research subject to licensing  
572 restrictions (in the case of proprietary citation data). For those interesting in generating our metrics over  
573 their own data or corpora, the titles and abstracts necessary to generate text-based metrics are openly  
574 available. The metrics of new concept births and mentions of concepts are relatively easy to compute,  
575 making it possible for anyone to compute metrics of radical generative work. The backward and forward  
576 Herfindahl indices of the breadth of mentions of new concepts have the same data requirements but  
577 are computationally more demanding. Thus, our text-based metrics of radical generative research,  
578 breadth of impact, and multidisciplinary should be accessible to most practitioners. Generating citation  
579 metrics requires a different type of data access, e.g., to Thomson Reuters' Science Citation Index as  
580 discussed here, or to one of the other citation databases. Calculating the mean citations to the works in  
581 a field-period pair, the quantiles of the citation distribution, and the variance of citations across the  
582 works in a field-period pair require total citation counts to articles exclusively and are not  
583 computationally demanding. These provide good measures of impact and riskiness. As indicated, the  
584 extreme right tail of citations (e.g., the 99.99<sup>th</sup> percentile of the citation distribution) is relatively  
585 strongly related to transformativeness and is not computationally burdensome either. The other citation  
586 metrics require data that go beyond raw forward citation counts, namely data on citing-cited article  
587 pairs. Backward citation ages and forward citation ages are both straightforward computationally,  
588 providing metrics of radical destructiveness and growth of impact. As with the text variables, the  
589 forward and backward citation Herfindahl's are more computationally burdensome. Thus, while users  
590 must generate the metrics that suit their data access and computational environment, the choices they  
591 face when implementing our methods are obvious.

592 There are a number of limitations related to the data used and the metrics defined in this study. First, all  
593 of our analyses are limited in topical focus to articles published in MEDLINE and are limited temporally  
594 to the period 1983-2012. In terms of citation data from the Web of Science corpus, we used all  
595 backward citations of articles published in 1983-2012 yet did not have access to forward citations  
596 beyond May 20, 2014. We used MEDLINE's titles and abstracts for the text-based metrics exclusively.

597 We used the MeSH hierarchy to measure the breadth of knowledge used in our target articles and the  
598 breadth of utilization of the ideas generated by our target articles and hence our definition of fields and  
599 our text-based metrics are restricted to the MeSH classification of the MEDLINE corpus. MEDLINE mostly  
600 covers biomedical research, a study of other research disciplines with different publication norms,  
601 researcher team sizes, and funding opportunities might provide different results. Given that our last  
602 period ends in 2012 and citation data ends in 2014 it is highly probable that the impact of some articles  
603 is still materializing. However, the results of our analysis seem robust as omitting the 2008-2012 period  
604 does not change values dramatically.

605 There are a number of directions for future work. First, we look to validate our metrics in a variety of  
606 ways. Specifically, we are implementing an online interactive interface that users can visit to identify  
607 highly transformative research by selecting any of the eleven metrics and associated parameter values.  
608 This will make it possible to solicit feedback on the accuracy, representativeness, and usefulness of the  
609 metrics from subject matter experts. We are also working to identify and engage subject matter experts  
610 in specific research to validate our metrics individually.

611 Beyond validation, there are a number of other important avenues for future research. First, we are  
612 interested in identifying the factors—from the funding mechanisms, to the demographics of the  
613 researchers in fields, to the networks of researchers—that lead to the production of transformative  
614 science. Second, we seek to attach analogous metrics to individual articles, not just to entire research  
615 fields in a given period as we have done here. Such estimates would allow us to identify specific  
616 transformative works. They would also allow us to identify features of research teams that are likely to  
617 produce transformative work.

## 618 Acknowledgements

619 We thank Mikko Packalen for helpful input on the text analysis and Neil Smalheiser and Vetle Torvik for  
620 the use of their Author-ity data and Thomson Reuters for access to Web of Science records. Sara  
621 Bouchard provided design expertise for optimizing the figures. All authors gratefully acknowledge  
622 support from P01 AG039347. Weinberg thanks NSF 1064220, 1348691, 1535399 and the Ewing Marion  
623 Kauffman and Alfred P. Sloan Foundations. Weinberg was supported on P01 AG039347 by the NBER  
624 directly and on a subaward from NBER to Ohio State. Börner and Light are partially supported by the  
625 National Science Foundation under award EAGER 1566393 and NCN CP Supplement 1553044 plus the  
626 National Institutes of Health under award U01CA198934. Any opinions, findings, and conclusions or  
627 recommendations expressed in this material are those of the author(s) and do not necessarily reflect the  
628 views of the National Science Foundation.

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668 **Appendix**

669 **A. Types and Metrics of Transformative Research**

670 The below table identifies different types of transformative research and maps them to eleven metrics

671 **Table A1.** Types and metrics of transformative research

National Science Board	NIH Roadmap	NSF	NIH Common Fund
<b>1. Generates New Paradigms and Scientific Fields</b>			
New paradigms or new scientific fields generating new ones [paradigms]	Create ... fundamental paradigms	Leads to the creation of a new paradigm ... provides pathways to new frontiers.	Create ... fundamental paradigms, bold, paradigm-shifting
<b>Metrics of generating important new concepts:</b> Concepts ( <i>Concepts</i> )—Introduction of heavily-used new concepts Mentions ( <i>BMentN</i> )—Use of important new concepts			
<b>2. Radical, Destroying Existing Paradigms</b>			
Radically different approaches or interpretations; overthrowing entrenched paradigms	Overturn fundamental paradigms	Radically change our understanding of an important existing scientific or engineering concept	Overturn fundamental paradigms
<b>Metrics of obsolescence of existing knowledge:</b> Backward Citation Age ( <i>BCiteAge</i> ) (negatively related)—The age of prior knowledge drawn on			
<b>3. Risky</b>			
	Inherently risky		Inherently risky
<b>Metrics of variation of new utilization of the knowledge generated:</b> Variance of Forward Citations ( <i>FCiteVar</i> )—Variation in utilization of knowledge produced			
<b>4. Multidisciplinary</b>			
Often can be multidisciplinary			
<b>Metrics of drawing on a wide range of knowledge</b> Backward Herfindahl of Citations ( <i>BHerfCite</i> )—Breadth of articles used Backward Herfindahl of Concepts ( <i>BHerfMentN</i> )—Breadth of important concepts used			
<b>5. Wide Impact</b>			
	Impact a broad area of biomedical research		
<b>Metrics of knowledge being used widely:</b> Forward Herfindahl Citations ( <i>FHerfCite</i> )—Herfindahl index of breadth of forward citations Forward Herfindahl Mentions ( <i>FHerfMent</i> )—Herfindahl index of breadth of future use of concepts introduced			
<b>6. Growing Impact</b>			
Often fragile in their early stages			
<b>Metrics of time path of utilization of knowledge:</b> Forward Citation Age ( <i>FCiteAge</i> )—Age of citations			
<b>7. High Impact</b>			
Scientific understanding	Profoundly impact ...		

advances dramatically	biomedical research		
<b>Metrics of citation impact:</b>			
Forward citation counts ( <i>FCiteMean</i> , <i>FCiteN</i> )—Number of citations			

672

## 673 B. Extracting and Processing Text

674 We first extract the title and abstract from each of the 22,376,811 records (articles) indexed in the 746  
675 MEDLINE 2014 Baseline XML Files including article identifying information such as PMID and Version.  
676 After extracting the title and abstract, we then index all words, word pairs and word triplets (1-, 2-, and  
677 3-grams). We then process the n-grams contained in these titles and abstracts by performing the  
678 following operations:

- 679 1. Convert all text to lower-case.
- 680 2. Eliminate 2- and 3-grams with words that cross the following characters: ,.?!\;)(\}\{[!-.
- 681 3. Eliminate all remaining characters that are not alphanumeric.
- 682 4. Eliminate all n-grams that contain words appearing in the stopwords list provided by the NLM at  
683 this address:
- 684 5. Eliminate all n-grams that contain the following character sequences: web, www, http, pubmed,  
685 MEDLINE.
- 686 6. Eliminate all n-grams that contain more than two adjacent numbers.
- 687 7. Eliminate all n-grams that have a length of less than three characters.
- 688 8. Keep all 1-grams with character length 3-29, 2-grams with character length 7-59, and 3-grams  
689 with character length 11-89.

690 Next, we stems each word from each n-gram using the module *Lingua::Stem* from the  
691 Comprehensive Perl Archive Network (CPAN). Finally, we index all the processed n-grams from  
692 each title and abstract into 746 tab-delimited text files corresponding to the 746 MEDLINE XML  
693 files.

694 As discussed in Section 3, only the 15,916,023 articles published in 1983-2012 are used to compute the  
695 text-based metrics. Here we focus on the 10,778,696 articles available in Thomson Reuters' Science  
696 Citation Index Expanded™ that match to MEDLINE.

## 697 C. Aggregating MeSH Terms to Construct Fields

698 We use the Medical Subject Headings (MeSH) that tag most articles in MEDLINE to characterize the  
699 fields to which each article belongs. There are 27,149 raw terms in the 2014 MeSH vocabulary and they  
700 vary widely in their descriptive detail. For instance, some articles are tagged with general terms such as  
701 "Body Regions" and some are tagged with more detailed terms such as "Peritoneal Stomata". Thus, in  
702 order to construct comparable fields, we aggregate all MeSH terms to a similar level of descriptive  
703 detail.

704 To understand our aggregation method, first note that MeSH terms have a hierarchical structure. At the  
705 top of the hierarchy (first-level terms) are 16 very general terms such as "Anatomy", "Organisms", and  
706 "Diseases" Each of these 16 first-level terms are identified by a unique capital letter. For instance,  
707 "Anatomy" is identified by the letter "A", "Organisms" is identified by "B", and so on. Beneath each of  
708 these first-level MeSH terms is a group of second-level MeSH terms. For instance, "Body Regions" is a  
709 second-level MeSH term beneath the top-level term "Anatomy". Each second-level MeSH term is  
710 identified by the capital letter of the first-level MeSH term it is beneath and by two numbers. For



711 instance, “Body Regions” is identified by “A01”. Beneath each second-level MeSH term is a group of  
712 third-level MeSH terms identified by the capital letter of the first-level term it is beneath, the two  
713 numbers of the second-level term it is beneath, and three subsequent numbers. For instance, “Anatomic  
714 Landmarks” is a third-level MeSH term under “Body Regions” and is identified as “A01.111”. This  
715 structure continues to depths of up to 12 levels.

716 Aggregating MeSH terms (that is, classifying lower level MeSH terms as a part of higher level MeSH  
717 terms) is not straightforward because some MeSH terms are beneath more than one higher level MeSH  
718 term and some articles can be tagged with multiple MeSH terms. Appendix Figure 2 illustrates our  
719 approach. Our handling of multiple levels is best illustrated by example. Consider the MeSH term  
720 “Dementia”. This MeSH term has two separate identifiers: “C10.228.140.380” and “F03.087.400”. Thus,  
721 this MeSH term falls under the first-level MeSH terms “Diseases” (identified by “C”) and “Psychiatry and  
722 Psychology” (identified by “F”). It also falls under the second-level terms “Nervous System Diseases”  
723 (“C10”) and “Mental Disorders” (“F03”). The problem arises because MEDLINE records only contain the  
724 MeSH terms themselves, not their identifiers. For instance, if a MEDLINE record is tagged with the MeSH  
725 term “Dementia”, we would not know if it was the “Dementia” that is beneath “Nervous System  
726 Diseases” or “Mental Disorders”.

727 If we wanted to aggregate all MeSH terms to the second-level, we would have to find a way to split  
728 “Dementia” between “Nervous System Diseases” and “Mental Disorders”. We opt for the  
729 straightforward method of assigning half to each higher level term. If we wanted to aggregate all MeSH  
730 terms to the fourth-level, “Dementia” would fall under the fourth-level term “Brain Diseases” (identified  
731 by “C10.228.140”) and “Dementia” itself (identified by “F03.087.400”). In this case, we still assign half of  
732 “Dementia” to “Brain Diseases” and half to “Dementia” itself. Finally, if we wanted to aggregate all  
733 MeSH terms to the fifth-level, “Dementia”, which has two fourth-level identifiers (“C10.228.140” and  
734 “F03.087.400”), is at a higher level of aggregation than the fifth-level. We deal with this by simply  
735 eliminating “Dementia”. It is too highly aggregated for our purposes.

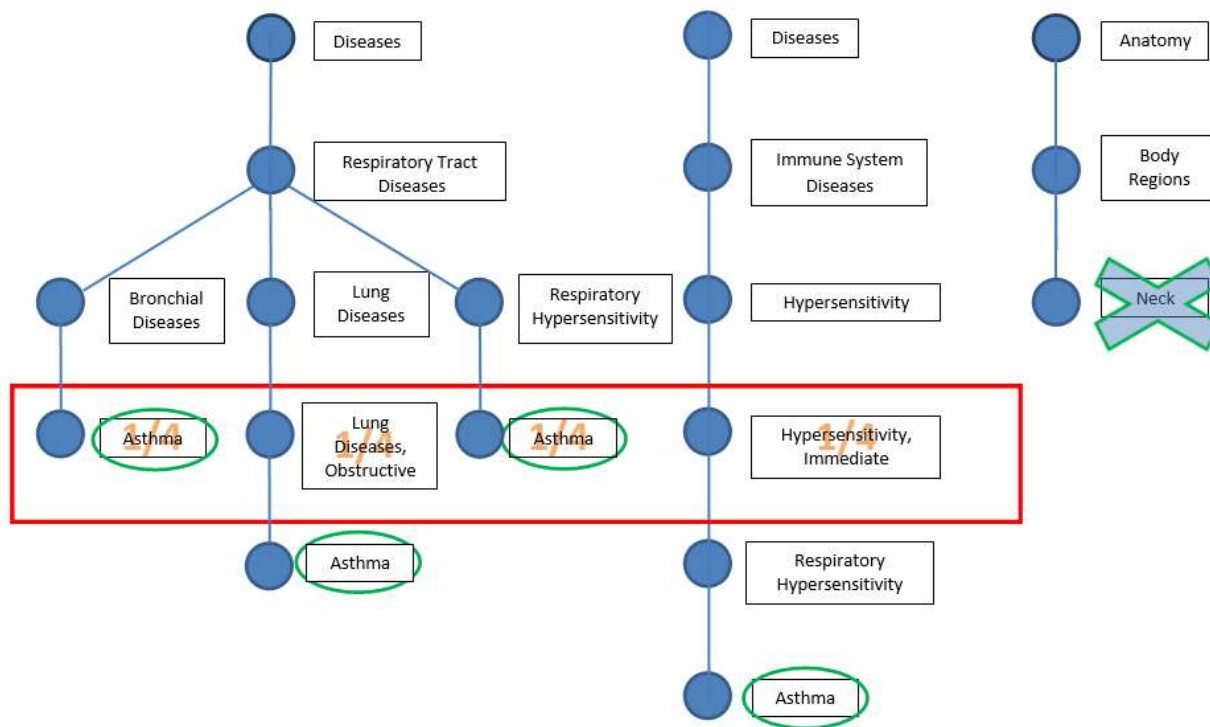
736 Our last step is to apportion each article indexed in MEDLINE to the newly aggregated MeSH terms.  
737 Again, examples are the most illustrative. Suppose we come across an article that is tagged by  
738 “Dementia” and we want to aggregate to the fourth-level. We know from above that half of Dementia  
739 would be assigned to “Brain Diseases” and half would be assigned to “Dementia” itself. However,  
740 suppose (as is usually the case) that this article is also tagged with other MeSH terms. Specifically,  
741 suppose that the article is also tagged with the fourth-, fifth- and ninth-level MeSH term “Health  
742 Information Exchange” (identified by “L01.700.253”, “L01.399.500.500”, “L01.313.500.500”, and  
743 “E05.318.308.940.968.625.500.500”). By the process discussed above, one fourth of “Health  
744 Information Exchange” will be assigned to each of the four fourth-level MeSH terms: “Health  
745 Information Exchange” itself (“L01.700.253”), “Health Information Management” (“L01.399.500”),  
746 “Medical Informatics” (“L01.313.500”), and “Data Collection” (“E05.318.308”).

747 We assume that each of the original MeSH terms, “Dementia” and “Health Information Exchange”  
748 receive equal weight in characterizing the article. Under this assumption, the article will be apportioned  
749 to each fourth level MeSH term as follows:

- 750 1.  $1/2 * 1/2 = 1/4$  to “Dementia”
- 751 2.  $1/2 * 1/2 = 1/4$  to “Brain Diseases”
- 752 3.  $1/2 * 1/4 = 1/8$  to “Health Information Exchange”
- 753 4.  $1/2 * 1/4 = 1/8$  to “Health Information Management”

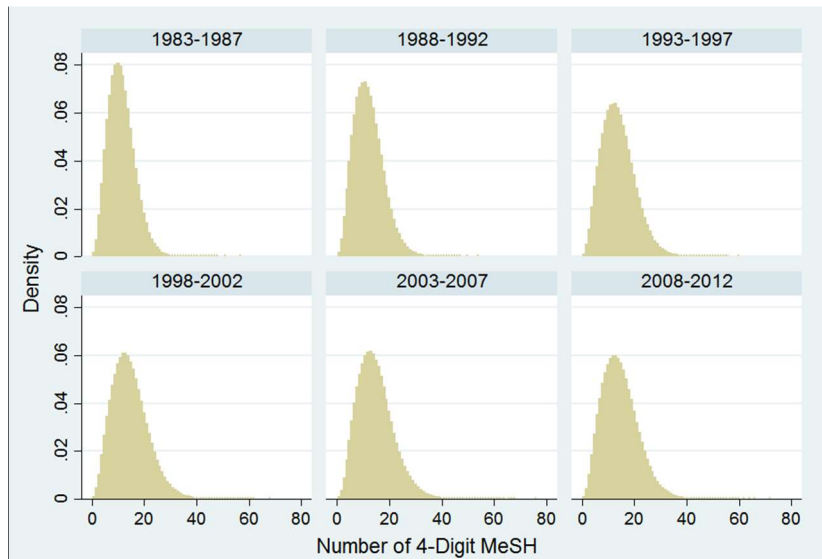
- 754 5.  $1/2 * 1/4 = 1/8$  to "Medical Informatics"
- 755 6.  $1/2 * 1/4 = 1/8$  to "Data Collection"

756  
 757 Obviously  $1/4 + 1/4 + 1/8 + 1/8 + 1/8 + 1/8 = 1$ . Thus, the article that was originally tagged by the two MeSH  
 758 terms "Dementia" and "Health Information Exchange" is now apportioned between six different fourth-  
 759 level MeSH terms. In general, we apportion each MEDLINE article across aggregated MeSH terms in two  
 760 stages. First, we equally apportion the original MeSH terms across the higher-level MeSH terms of which  
 761 they are a part (e.g. apportion "Dementia" equally across "Brain Diseases" and "Dementia"). Second, we  
 762 weight this apportionment by the inverse of the number of original MeSH terms that tag the article (e.g.  
 763 our hypothetical article was tagged by two original MeSH terms, and so we weight by  $1/2$ ).



764  
 765 **Figure C.1:** Process used to aggregate MeSH terms in order to construct fields. Example shows MeSH  
 766 terms Asthma and Neck.

767 Figure C.2 plots the distribution of 4-digit MeSH terms per article for the six different time periods. The  
 768 number of MeSH terms assigned to articles increases over time.



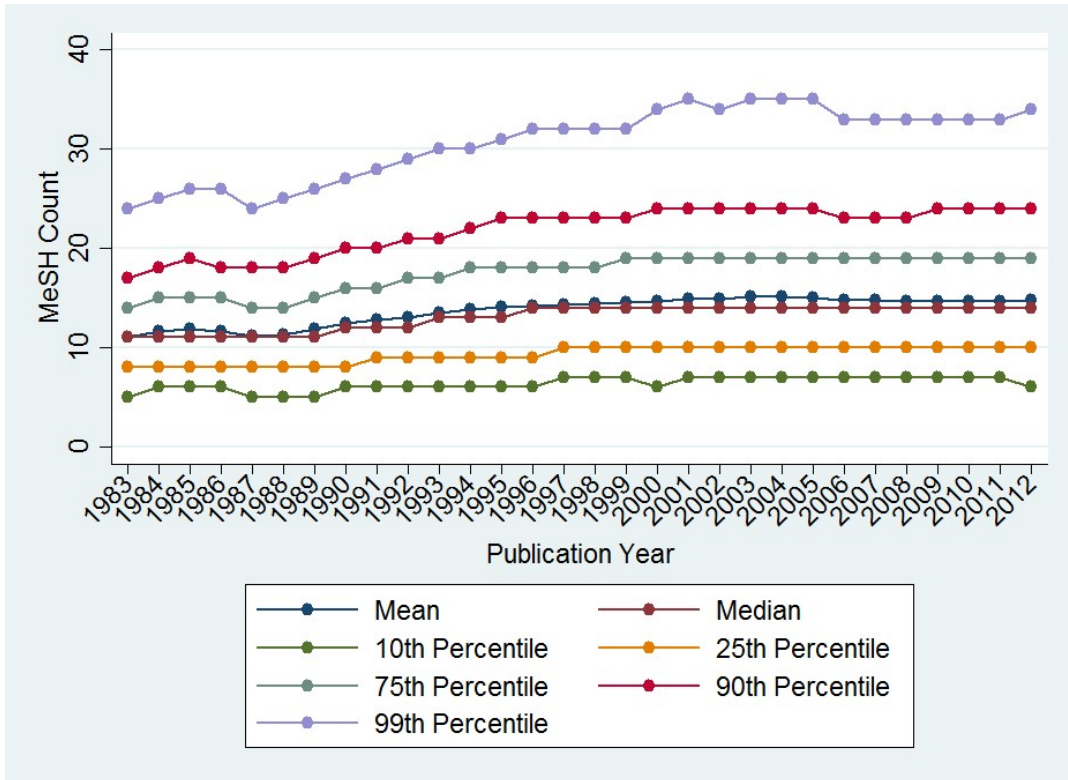
769

770

771 **Figure C.2:** Distribution of the number of 4-digit MeSH terms per article.

772

773 Figure C.3 shows the mean number of MeSH4 terms as well as selected quantiles (the 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>,  
 774 75<sup>th</sup>, 90<sup>th</sup>, and 99<sup>th</sup> quantiles) of the distribution of the number of terms. The mean and median number  
 775 of MeSH4 terms increases from roughly 10 per article in the 1970s to roughly 12 in 1974 after which the  
 776 number of MeSH4 terms dips before gradually increasing to roughly 12 after 2000. In addition to the  
 777 upward trend there is an increase in dispersion of the number of MeSH4 terms, with no increase in the  
 778 10<sup>th</sup> and 25<sup>th</sup> quantiles in the most recent years.



779

780 **Figure C.3:** Quantiles of the distribution of the number of MeSH4 terms per article by publication year.

781 **D. Formal Definition of Metrics**

782 The below table gives the formal description of each metric defined at the field-period level. A bin  $b$  is  
 783 defined by a field-period pair;  $i$  indexes articles in bin  $b$ ;  $w_i$  is the fraction of article  $i$  allocated to the  
 784 MeSH4 field of  $b$ ; and  $forward$  ( $backward$ )  $citation\ count_i$  is article  $i$ 's forward ( $backward$ ) citation  
 785 count.

786 **Table D.1:** Formal definition of field-period metrics

<b>1. Radical - Generative</b>	
Concepts	<p>Let <math>\mathbb{C}</math> be the set of all top concepts.<sup>1</sup> Let <math>\mathbb{A}^{pc}</math> be the set of all articles published in time period <math>p</math> that use concept <math>c \in \mathbb{C}</math> in the first year it is used, its “vintage year”. Let <math>A^{pc} = \#\mathbb{A}^{pc}</math> be the number of articles in the set <math>\mathbb{A}^{pc}</math>. Consider article <math>a \in \mathbb{A}^{pc}</math>. Define <math>\alpha_{af}</math> as the fraction of article <math>a</math> that belongs to field <math>f</math>. Then the fraction of concept <math>c</math> that belongs to field <math>f</math> is given by <math>\gamma_{fpc} = \frac{1}{A^{pc}} \sum_{a \in \mathbb{A}^{pc}} \alpha_{af}</math>. Finally, the total number of top concepts that originate in field <math>f</math> in time period <math>p</math> is given by <math>concepts_{fp} = \sum_{c \in \mathbb{C}} \gamma_{fpc}</math>.</p>
BMentN	<p>Let <math>\mathbb{C}</math> be the set of all top concepts. Let <math>\mathbb{A}^{pcN}</math> be the set of all articles published in time period <math>p</math> that use concept <math>c \in \mathbb{C}</math> within <math>N</math> years of its vintage year. Consider article <math>a \in \mathbb{A}^{pcN}</math>. Define <math>\alpha_{af}</math> as the fraction of article <math>a</math> that belongs to field <math>f</math>. Then the total number times that field <math>f</math> uses concept <math>c</math> within <math>N</math> years of its vintage is given by <math>n_{fpcN} = \sum_{a \in \mathbb{A}^{pcN}} \alpha_{af}</math>. Finally, the total number of top concept mentions that belong to field <math>f</math> in time period <math>p</math> is <math>BMentN_{fpN} = \sum_{c \in \mathbb{C}} n_{fpcN}</math>.</p>
<b>2. Radical - Destructive</b>	
BCiteAge	<p>Consider an article <math>j</math> that is cited by article <math>i</math>. The age of the citation to article <math>j</math> is backward citation age <math>age_{ij} = i</math>'s publication year <math>- j</math>'s publication year and article <math>i</math>'s average backward citation age is</p> $\text{average backward citation age}_i = \frac{1}{M_i} \sum_j \text{backward citation age}_{ij}$ <p>where <math>M_i</math> is the number of backward citations for paper <math>i</math>.<sup>2</sup> Then the backward citation age among articles in bin <math>b</math> (i.e. some field period pair) is</p> $BCiteAge_b = \frac{1}{\sum_{i \in b} w_i} \sum_{i \in b} w_i \times (\text{average backward citation age}_i),$ <p>where <math>w_i</math> gives the share of weight on article <math>i</math> among all articles in bin <math>b</math>.</p>
<b>3. Risky</b>	
FCiteVar	<p>Suppose there are <math>K_b</math> articles in bin <math>b</math>,</p> $FCiteVar_b = \frac{1}{K_b} \sum_{i \in b} (\text{forward citation count}_i - FCiteMean_b)^2.$
<b>4. Multidisciplinary</b>	
BHerfCite	<p>Let <math>\pi_{if}</math> be the set of articles in field <math>f</math> that article <math>i</math> cites. Then the weighted number of articles from field <math>f</math> that article <math>i</math> cites is <math>\sum_{k \in \pi_{if}} w_k</math>, where <math>w_i</math> gives the share of weight on article <math>i</math> among all articles in field <math>f</math>.</p>

	<p>Each article contributes to the backward citation count in bin <math>b</math> according to its bin <math>b</math> weight. Thus the number of citations from all articles in bin <math>b</math> to articles in field <math>f</math> is</p> $R_b^f = \sum_{i \in b} w_i \sum_{k \in \pi_{if}} w_k.$ <p>Summing <math>R_b^f</math> over all cited fields gives the total number of citations from articles in bin <math>b</math>,</p> $R_b = \sum_{i \in b} w_i \sum_f \sum_{k \in \pi_{if}} w_k.$ <p>Let <math>\omega_b^f = \frac{R_b^f}{R_b}</math> be the share of <math>b</math>'s backward citations to field <math>f</math>. Then</p> $\text{BHerfCite}_b = 1 - \sum_f (\omega_b^f)^2.$
BHerfMentN	<p>Let <math>\mathbb{C}</math> be the set of all top concepts.<sup>1</sup> Let <math>\mathbb{A}^{pCN}</math> be the set of all articles published in time period <math>p</math> that use concept <math>c \in \mathbb{C}</math> within <math>N</math> years of its vintage year. Consider article <math>a \in \mathbb{A}^{pCN}</math>. Define <math>\alpha_{af}</math> as the fraction of article <math>a</math> that belongs to field <math>f</math>. Then the total number of times that field <math>f</math> in period <math>p</math> uses concept <math>c</math> within <math>N</math> years of its vintage is given by <math>n_{fpNc} = \sum_{a \in \mathbb{A}^{pCN}} \alpha_{af}</math>. The total number of that field <math>f</math> in period <math>p</math> uses any concept within <math>N</math> years of its vintage is given by <math>m_{fpN} = \sum_{c \in \mathbb{C}} n_{fpNc}</math>. The Herfindahl for field <math>f</math> in period <math>p</math> is given by <math>herf_{fpN} = 1 - \sum_{c \in \mathbb{C}} (n_{fpNc} / m_{fpN})^2</math>.</p>
<b>5. Wide Impact</b>	
FHerfCite	<p>Let <math>\theta_{if}</math> be the set of articles in field <math>f</math> that cite article <math>i</math>. Then the number of articles from field <math>f</math> that cite article <math>i</math> is</p> $\sum_{j \in \theta_{if}} w_j.$ <p>Each cited article contributes to the total forward citation count in bin <math>b</math> according to its bin <math>b</math> weight. Thus the number of citations from field <math>f</math> to all articles in bin <math>b</math> is</p> $C_b^f = \sum_{i \in b} w_i \sum_{j \in \theta_{if}} w_j.$ <p>Summing <math>C_b^f</math> over all citing fields gives the total number of citations to articles in bin <math>b</math>,</p> $C_b = \sum_{i \in b} w_i \sum_f \sum_{j \in \theta_{if}} w_j.$ <p>Let <math>s_b^f = \frac{C_b^f}{C_b}</math> be the share of <math>b</math>'s forward citations in field <math>f</math>. Then</p> $\text{FHerfCite}_b = 1 - \sum_f (s_b^f)^2.$
FHerfMent	<p>Let <math>\mathbb{C}^v</math> be the set of all top concepts with a vintage <math>v</math>. Let <math>\mathbb{A}^c</math> be the set of articles that use concept <math>c \in \mathbb{C}^v</math> in the vintage year <math>v</math>. Consider an article <math>a \in \mathbb{A}^c</math>. Define <math>\alpha_{af}</math> as the fraction of article <math>a</math> that belongs to field <math>f</math>. Then the fraction of concept <math>c</math> that belongs to field <math>f</math> is <math>\gamma_{cf} = \frac{1}{A^c} \sum_{a \in \mathbb{A}^c} \alpha_{af}</math>.</p>

	<p>Let <math>\mathbb{A}_\infty^c</math> be the set of articles that <i>ever</i> use concept <math>c \in \mathbb{C}^v</math>. Then the number of times that field <math>g</math> ever mentions concept <math>c</math> is given by <math>n_{cg\infty} = \sum_{a \in \mathbb{A}_\infty^c} \alpha_{ag}</math>.</p> <p>The Herfindahl index is given by</p> $herf_{fv} = 1 - \sum_{g \in \mathbb{F}} \sum_{c \in \mathbb{C}^v} \left\{ \left[ \frac{\gamma_{cf} \times n_{cg\infty}}{\sum_{g \in \mathbb{F}} \sum_{c \in \mathbb{C}^v} (\gamma_{cf} \times n_{cg\infty})} \right]^2 \right\}$
<b>6. Growing Impact</b>	
FCiteAge	<p>Consider an article <math>i</math> that is cited by article <math>j</math>. The age of the citation from article <math>j</math> is</p> <p><i>forward citation age</i><math>_{ij} = j</math>'s publication year <math>- i</math>'s publication year</p> <p>and article <math>i</math>'s average forward citation age is</p> $\text{average forward citation age}_i = \frac{1}{N_i} \sum_j \text{forward citation age}_{ij}$ <p>where <math>N_i</math> is the number of forward citations for paper <math>i</math>.<sup>2</sup></p> $\text{FCiteAge}_b = \frac{1}{\sum_{i \in b} w_i} \sum_{i \in b} w_i \times (\text{average forward citation age}_i).$
<b>7. High Impact</b>	
FCiteMean	$\text{FCiteMean}_b = \frac{1}{\sum_{i \in b} w_i} \sum_{i \in b} w_i \times (\text{forward citation count}_i).$
FCiteN	<p>Order the <math>K_b</math> articles in bin <math>b</math> by forward citation count. Index the ordered articles by <math>j = 1, 2, \dots, K_b</math> where <math>j = 1</math> corresponds to the article with the highest forward citation count, <math>j = 2</math> corresponds to the second highest citation count, and so on. Then compute,</p> <p><math>\text{FCiteN}_b = \text{forward citation count}_z</math> where <math>z</math></p> $= \operatorname{argmin}_j \left\{ j, \text{satisfies } \sum_{i=1}^j w_i \geq \left(1 - \frac{N}{100}\right) \sum_{k \in b} w_k \right\}.$
<p>Notes:</p> <ol style="list-style-type: none"> <li>1. Top Concepts: Top concepts defined as one of the 10,128 most highly used 1-, 2-, or 3-grams that first appeared in a MEDLINE title or abstract between 1983 and 2012.</li> <li>2. FCiteAge: <i>forward citation age</i><math>_{ij}</math> is set to missing if either the value is negative or if <math>j</math>'s publication year is not valid. <math>N_i</math> is the number of forward citations to article <math>i</math> that have non-missing ages.</li> </ol>	

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